

$$1) y = \frac{\ln(\lg(\sin(e^{-x})))}{-e^2};$$

$$2) y = \frac{\sin(\ln(3x)) \cdot \sqrt[3]{\arcsin(-2x^2)}}{-2};$$

$$3) y = \frac{\operatorname{arcctg}^2(2-x^2)}{3-\cos(2x)};$$

Ats.:

$$1. y' = \frac{1}{-e^2} \cdot \frac{1}{\lg(\sin(e^{-x}))} \cdot \frac{1}{\sin(e^{-x})\ln(10)} \cdot \cos(e^{-x}) \cdot e^{-x} \cdot (-1);$$

$$2. y' = (uv)' = u'v + uv' = \frac{1}{-2} \cdot \left(\cos(\ln(3x)) \cdot \frac{1}{3x} \cdot 3 \cdot \sqrt[3]{\arcsin(-2x^2)} + \right. \\ \left. \sin(\ln(3x)) \cdot \frac{1}{3} (\arcsin(-2x^2))^{-\frac{2}{3}} \cdot \frac{1}{\sqrt{1-(-2x^2)^2}} \cdot (-4x) \right);$$

$$3. y' = \left(\frac{u}{v} \right)' = \frac{u'v - uv'}{v^2} = \\ \frac{2\operatorname{arcctg}^2(2-x^2) \cdot \left(-\frac{1}{1+(2-x^2)^2} \right) \cdot (-2x) \cdot (3-\cos(2x)) - \operatorname{arcctg}^2(2-x^2) \cdot \sin(2x) \cdot 2}{(3-\cos(2x))^2}$$